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Optimal power flow solution using adaptive tabu search

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This paper illustrates an application of adaptive tabu search (ATS) to optimal power flow (OPF) problems in comparison with some effective mathematical and evolutionary optimization methods. Although, the ATS was originally developed for solving a combinatorial optimization problem whose parameters are discrete, it has the ability to handle continuous variables by treating them as discrete ones with a very small variable step-size to gain accuracy. The proposed algorithm was tested with 9-bus and 300-bus test systems to represent a small-scale and a comparatively large-scale power system, respectively. Each test power system was challenged by performing three test cases. The first test case was given by applying a quadratic function to generators’ fuel-cost curve, whereas a non-smooth fuel-cost function was assigned to the second. In addition, the system voltage profile was considered and set as the objective function to be minimized in the last test case. The comparisons among solutions obtained by sequential quadratic programming (SQP), evolutionary programming (EP) and the ATS were carried out, from which satisfactory results and the selection of solution methods to OPF problems were summarized.

Key words: Optimal power flow problem, sequential quadratic programming, evolutionary programming, adaptive tabu search, quadratic fuel cost, non-smooth fuel cost.

INTRODUCTION

To date, an electrical power system is very large and obviously complicated due to technological enhancement of power system engineering. Increase of electrical energy consumption often leads to extending and upgrading an existing power transmission and distribution network to serve all customers sufficiently, effectively and economically. To achieve good performance for power delivery, a real power dispatching problem must be taken into account in order to minimize total generation cost (El-Abiad and Jaimes, 1969). Also, appropriate reactive power flows relate to power losses and system voltage profiles, directly. In this viewpoint, tap setting of under-load tap-changing transformers (ULTCs), voltage magnitude of voltage-controlled buses or installing re-active power sources can improve voltage characteristics and reduce power losses considerably (Mansour and Abdel, 1984). Dommel and Tinney (1968) proposed the method of optimal power flow (OPF), which employs allocation of real power generated by generators to co-operate with controlling ULTCs, magnitude of voltage-controlled buses or reactive power sources for minimizing the system objective.

As a general approach, a typical OPF problem employs an optimization method for balancing the power flow equations and finding the optimum solution. The solution satisfies the constraint of the minimum value of an objective function, that is, total generation cost for most cases, within the entire search space. The OPF problem is in general non-convex and non-linear. It may exist in many local minima. Many mathematical techniques have been developed and applied to this problem such as linear programming, interior point method, etc., (Wood and Wollenburg, 1996). The algorithms essentially need some problem simplification such that the problem is linear or convex. Thus, a true global minimum cannot be guaranteed. Then, stochastic optimization methods such as genetic algorithms (GAs), simulated annealing (SA), artificial neural network (ANN) and evolutionary
Simulations were conducted by using MATHPOWER software package. Tangpatiphan and Yokoyama (2008) presented the problem of reactive power planning (RPP) taking into account the principles of economics and reliability as its objective. This work used some efficient mathematical programs, such as the steepest descent method, the quadratic programming and the gradient projection method. Leung et al. (2000) proposed a genetic algorithm (GA) for solving optimal power flow problems in power systems which are equipped with flexible AC transmission systems (FACTS). Abido et al. (2002a) proposed the optimal power flow solution by using tabu search method (TS). The test was simulated by using the IEEE 30-bus test system with four test cases. The result of this simulation concluded that tabu search method is capable to solve optimal power flow problem with the lowest objective function and the fastest convergence. Abido (2002b) proposed a power flow optimization by means of particle swarm optimization (PSO). This work was carried out by simulating the IEEE 30-bus test system with the fuel-cost function is the system objective. Gaing (2005) employed the mixed-integer particle swarm optimization (MIPSO) for solving optimal power flow problems with a combination of continuous and discrete control variables. The total production cost with smooth and non-smooth curves was used as the system objective to be minimized. The IEEE 9-bus and 26-bus test power systems were challenged. Vaisakb and Srinivas (2005) proposed optimal power flow solutions by using differential evolution (DE), which was tested in the IEEE 30-bus test system with fuel-cost objective functions. Younes et al. (2007) proposed the optimal power flow solutions using genetic algorithms. The IEEE 57-bus test system was used together with the total production cost as the objective function. The simulations were conducted by using MATHPOWER software package. Tangpatiphan and Yokoyama (2008) presented evolutionary programming with artificial neural network by solving the transient stability based optimal power flow problems. The swing equation and the rotor angle dynamic were determined. The IEEE 30-bus test system was used for the test. Wenjuan et al. (2008) presented the problem of reactive power planning (RPP) to determine the optimal location and the size of the reactive power sources. This work included the consideration of (1) the ability of power transfer capability, (2) fuel-cost minimization and (3) the voltage stability enhancement. Oumarou et al. (2009) presented the optimal power flow solution by using the particle swarm optimization. The IEEE 30-bus test power system was used for the test to adjust generators’ powers, bus voltage magnitudes, reactive powers from the var sources and transformer taps. Tangpatiphan et al. (2009) presented the evolutionary programming for solving the optimal power flow problem with consideration of steady-state voltage stability. The system objective function was the total production cost with system security and voltage stability constraints. In this paper, the IEEE 30-bus test system was employed. Va et al. (2010) presented the optimal power flow solution using some efficient intelligent search methods. Genetic algorithms, differential evolution and ant colony optimization (ACO) were challenged with the IEEE 30-bus test system.

These methods can successfully manipulate a problem in non-convex or non-linear. Therefore, an obtained optimal solution is more accurate and realistic. Unfortunately, these algorithms normally take lengthy calculation time when compared with the mathematical optimization methods. Since the beginning of the previous decade, tabu Search (TS) and its variants, such as adaptive tabu search (ATS) have been introduced and performed drastically improved search performance. Regarded as one of the random search processes, ATS provides a near global minimum by successfully avoiding local-minimum traps. Successful applications of the ATS have emerged (Mantawy et al., 1998; Mori and Hayashi, 1998; Mori and Ogita, 1999a; Mori and Sone, 1999b; Denna et al., 1999; Kulworawanichpong and Sujijitorn, 2002; Abido, 2002a; Lin et al., 2002). Although, ATS algorithm was developed as a stochastic optimization technique, it can find an optimal solution within a short calculation time. Consequently, this paper applied ATS for solving the OPF problem.

PROBLEM FORMULATION

The OPF problem is a problem that considers dispatching real power among power generation plants sufficiently, effectively and economically together with reactive power-flow control to gain the minimum for some particular objective, normally the total generation cost. The OPF is in nature non-convex and non-linear; there exist many local minima that can trap an inefficient optimization method. Due to largely sizing and complexity of the OPF formulation in the past where a high-speed computer was rare, it could be decomposed into two consecutive sub-problems, such as P- and Q-problems (Shouls and Sun, 1982). However, with continuously emerging high-speed computer technologies within the last two decades ago, a digital computer nowadays is able to handle bulky and very complicated problems. To combine the P- and Q-problems together, a set of control variables must be re-formed by combining all control variables altogether from both sub-problems. The
combined OPF formulation is defined by the following explanation.

The main objective focuses on minimizing the total generation cost by considering real power output of all controlled generators, tap position of ULTCs, voltage magnitudes of the slack bus and voltage-controlled buses or reactive powers injected by reactive power sources as control variables (Wood and Wollenburg, 1996). Assuming that a given power system has the following properties, containing \( N_{PV} \) voltage-controlled buses and \( N_{T} \) ULTCs.

Let \( \tilde{u} \) be a control variable and be defined by:

\[
\tilde{u} = \begin{bmatrix} P_{G_i} \\ V_j \\ V_{ref} \\ T_p \end{bmatrix}
\]

Where

\[
P_{G_i} \sim [P_{G_i}^{\min}, P_{G_i}^{\max}]; \ i=1,2,...,N_{G} -1
\]

\[
V_j \sim [V_j^{\min}, V_j^{\max}]; \ j=1,2,...,N_{PV}
\]

\[
T_p \sim [T_p^{\min}, T_p^{\max}]; \ p=1,2,...,N_{T}
\]

\[
V_{ref} \sim [V_{ref}^{\min}, V_{ref}^{\max}]
\]

The formulation of the OPF problem is given as:

Minimize \( F_T = \sum_{i=1}^{N_d} f(P_{G_i}) \) 

Subjects to

1. Equality constraints: power mismatch equations:

\[
P_{sch,k} = \sum_{i=1}^{N_B} |Y_{ik}| V_{i} V_{k} \cos(\theta_{ik} + \delta_k - \delta_i) = 0
\]

\[
Q_{sch,k} = \sum_{i=1}^{N_B} |Y_{ik}| V_{i} V_{k} \sin(\theta_{ik} + \delta_k - \delta_i) = 0
\]

2. Inequality constraints: limits of control or state variables

\[
P_{G_i}^{\min} \leq P_{G_i} \leq P_{G_i}^{\max}
\]

\[
Q_{G_i}^{\min} \leq Q_{G_i} \leq Q_{G_i}^{\max}
\]

\[
V_j^{\min} \leq V_j \leq V_j^{\max}
\]

\[
T_p^{\min} \leq T_p \leq T_p^{\max}
\]

\[
V_{ref}^{\min} \leq V_{ref} \leq V_{ref}^{\max}
\]

Voltage variations for all load buses to find optimal solutions for the OPF problem, an appropriate optimization method has to be chosen to handle its non-linear and non-convex nature. In fact, although there is no restriction for making selection, searching speed and accuracy are mainly the matter of concern. This paper attempts to demonstrate the effectiveness of three different optimization techniques, namely SQP, EP and ATS. Here, only sequential quadratic programming (SQP0 and EP are discussed.

The general form of a non-linear optimization problem (Nash and Sofer, 1996) can initially be expressed as follows:

Minimize \( f(x) \)

Subjects to \( g_i(x) = 0 \); for \( i = 1, 2, ..., M \)

\( h_j(x) \leq 0; \) for \( i = M_E + 1, ..., M \)

\( l \leq x \leq u \)

\( f(x) \) is the objective function describing the mathematical formula of the aim. \( u \) and \( l \) are upper and lower bounds of the variable \( x \), respectively.

Sequential quadratic programming

The SQP algorithm is a generalization of Newton's method for an unconstrained optimization. At any iteration \( k \), the SQP employs quadratic approximation to characterize the objective function in the following expressions (Nash and Sofer 1996; MathsWork, 2001):

Minimize \( [\nabla f(x_k)]^T d_k + \frac{1}{2} d_k^T \nabla^2 L(x_k, \lambda_k) d_k \) 

(4)

Subjects to:

\( c_i(x_k) + [\nabla c_i(x_k)]^T d_k = 0; \ i = 1,2,...,M_E \)

(5)

\( c_i(x_k) + [\nabla c_i(x_k)]^T d_k \leq 0; \ i = M_E + 1, ..., M \)

(6)

where \( L(x, \lambda) = f(x) + \sum_{i=1}^{M} \lambda_i c_i(x) \).

As can be seen from the aforementioned expressions, the Hessian matrix needs to be updated at every iteration. In addition, this matrix must be a positive definite matrix to ensure its convergence. Thus, the Broyden-Fletcher-Goldfarb-Shanno (BFGS) approximation \( B_k \) is used to replace the Hessian matrix at each iteration and can be updated by using the following formula (Nash and Sofer, 1996):

\[
B_{k+1} = B_k - \frac{B_k s_k s_k^T B_k}{s_k^T B_k s_k} + y_k y_k^T
\]

(7)

\[
s_k = x_{k+1} - x_k
\]

(8)

\[
y_k = \nabla L(x_k, \lambda_k) - \nabla L(x_k, \lambda_k)
\]

(9)

To find the step \( d_k \), a line search must be applied. Unlike the unconstrained optimization where the optimal step length can be chosen by minimizing the objective function directly along a given
search direction, it needs to satisfy all the constraints at the same time. This often causes conflict and usually makes obtained solutions infeasible. So, it is necessary to include these criteria. To avoid this conflict, the merit or penalty function is applied as follows (MathWorks, 2001):

\[ M(x,v) = f(x) + \sum_{i=1}^{M} v_i \| c_i(x) \| + \sum_{i=M+1}^{M_k} \max \{ c_i(x), 0 \} \]  

(10)

Although, there are some other forms of the merit function such as the augmented Lagrangian merit function, Equation 10 was used MATLAB’s optimization toolbox, which is the reference for the SQP-based optimizer used in this paper.

When \( x_k \) and \( d_k \) have already been attained somehow from the previous iteration, the \( x_{k+1} \) was computed by \( x_{k+1} = x_k + \alpha_k d_k \), where the step length \( \alpha_k \) is to minimize the merit function in the form of \( M(x_k + \alpha_k d_k, v) \). By repeating these processes, solutions found obviously satisfied all constraints while minimizing the objective function. Nevertheless, this generated sequence converges to a local minimum only due to the use of gradient information.

**Evolutionary programming**

Evolutionary programming was invented by Fogel et al. (1966). At this time, artificial intelligence was limited to two main avenues of investigation: modeling the human brain or neural networks and modeling the problem solving behavior of human experts or heuristic programming. Both focused on emulating humans as the most advanced intelligent organism produced by evolution. The alternative, envisioned by Fogel, was to refrain from modeling the end product of evolution, but rather to model the process of evolution itself as a vehicle for producing intelligent behavior. Fogel et al. (1966) viewed intelligence as a composite ability to make predictions in an environment coupled with the translation of each prediction into a suitable response in light of a given goal (for example, to maximize a payoff function). Thus, the viewed prediction is a prerequisite for intelligent behavior. The modeling of evolution as an optimization process was a consequence of Fogel’s expertise in the emerging fields of biotechnology (at the time evolution as an optimization process was a consequence of Fogel’s predictions in an environment coupled with the translation of each alternative, envisioned by Fogel, was to refrain from modeling the end product of evolution, but rather to model the process of evolution itself as a vehicle for producing intelligent behavior. The modeling of evolution as an optimization process was a consequence of the TS method that searches for the best solution by moving from a current solution to find a better solution repeatedly. One of the important features of the TS method is its tabu list that keeps the history of search paths. The information in the list is used for finding a new direction of search movement. Every ‘new’ is expected to search for a better solution and ultimately the optimum one. Another feature of the tabu search method is its aspiration criterion. The aspiration criterion provides preferable characteristics of any possible solutions. It is particularly useful for the selection of a
we have proposed two additional mechanisms namely backtracking and adaptive search radius. The enhanced version of the tabu search method has been named the adaptive tabu search (Kulworawanichpong et al., 2004; Pungdownreung et al., 2007). Regarding to the intensification mechanism, the back-tracking mechanism allows the search to look backward to some previous solutions stored in the tabu list. This mechanism may become necessary when the search encounters an entrapment caused by a local solution. An alternative solution is then chosen from the current and the previous solutions. With the back-tracked solution, a new search space is created. Given this new search space to explore, the search moves in a new direction away from that approaching the local solution. Note that the new solution chosen here is not necessary to be the best solution within the current search space but it helps the search to escape from an entrapment.

As shown in Figure 2, from the starting point \( x_1 \), a neighborhood \( N(x_1) \) given as a set of point around \( x_1 \) with a certain radius \( r \) is randomly generated. The best solution \( x_2 \) among them is selected randomly for creating the next neighborhood \( N(x_2) \) and is also put into the TL if it is not there before. However, the forbidden that moves in the TL can be released if some conditions are satisfied according to aspiration criteria. This method can be performed step-by-step as follows:

1. Generate randomly an initial solution \( x_0 \) from the feasible set. Set \( x_0 \) is an initial optimal solution.
2. Create randomly a neighborhood of a current optimum. As briefly described in the abstract, the TS was developed based on a discrete-variable problem. Applying the TS to a continuous-variable search space needs some modification. With a radius \( r \) given by the Equation 4 and shown in Figure 3, each member of the neighborhood is defined by

\[
x = x_1 + \alpha r (x_{\text{max}} - x_{\text{min}})
\]

(15)

where \( \alpha \) is a random number generated in the range of \([-1, 1]\), \( x_1 \) is a previously visited solution and \( x_0 \) is a randomly generated member of neighborhood.

3. Let \( x_0 \) be the best solution in the neighborhood. Update the TL if

Figure 1. Flowchart of the EP procedure.

Figure 2. Search space and neighborhood of ATS.

Figure 3. Radius of a neighborhood.
OPTIMAL POWER FLOW SOLUTION USING ADAPTIVE TABU SEARCH

To apply the ATS algorithm to an OPF problem, all relevant variables must be re-defined in discrete form with a very small variable step-size. It notes that, throughout the paper, variable step-sizes of power output, voltage-magnitude at controlled buses and ULTC tap are all set to be $1 \times 10^{-4}$ p.u. for all test cases.

As all neighborhood of a current solution are not explored, a certain number of the neighborhood members are chosen to form candidate to the next move. So, $N_{nh}$ is set as 10 in this paper. Also, the radius of neighborhood is selected at $r = 0.10$. To precede the TS method, TL and AC must be specified. These two parameters critically depend on the nature of problems and they could be varied when a different system is applied. In this paper, TL is capable to store previously visited solutions up to 10 places, 5 to 30 is suggested by Lin et al. (2002). When the searching process is trapped at a local minimum, the AC is activated to release forbidden moves to gain better solutions. In this paper, after 10 moves, if the best solution obtained thus far cannot be improved, then it releases the forbidden move.

The OPF based on the ATS method consists of the following procedures.

START:
- Set the counter $k = 0$
- Randomly generate an initial feasible solution

$$\bar{u}_k = [p_{gi}^{(k)}, v_j^{(k)}, v_j^{(k)}]$$

LOOP:
1) Randomly generate $\bar{u}_k^{(q)} \in N(\bar{u}_k)$ for $q = 1.N_{nh}$
   - $p_{gi}^{(q)} = p_{gi}^{(k)} + \alpha \cdot r \cdot (p_{gi}^{\text{max}} - p_{gi}^{\text{min}})$, $i=1,2,..., N_G$
   - $v_j^{(q)} = v_j^{(k)} + \alpha \cdot r \cdot (v_j^{\text{max}} - v_j^{\text{min}})$, $i=1,2,..., N_P$
   - $v_r^{(q)} = v_r^{(k)} + \alpha \cdot r \cdot (v_r^{\text{max}} - v_r^{\text{min}})$
   - $T_p^{(q)} = T_p^{(k)} + \alpha \cdot r \cdot (T_p^{\text{max}} - T_p^{\text{min}})$, $i=1,2,..., N_T$

2) Evaluate feasibility and the objective function of candidates for $q = 1.N_{nh}$
   - Solving power flow equations
   - Checking feasibility
   - Evaluate the objective function if it is feasible
3) Obtain the best solution from the candidates
   - Check for the forbidden move
   - Check AC satisfaction
   - Accept the solution and update TL if satisfied
4) Check the termination criteria
   - If satisfied, Update the counter and go to LOOP
   - Otherwise, Go to STOP

STOP:
- The optimal solution is already obtained
- The searching process is terminated.
SIMULATION RESULTS

Although, modern electric power system consists of many types of power plants, in this research, the tests focused on fossil power generation units only. A simple model of such a generator is made from its input fuel cost in $/h and corresponding power output was generated in MW as input and output variables, respectively.
The objective to be minimized is the fuel cost function of each generator. The fuel cost function can be represented as a quadratic function with a valve-point loading function, as shown in Figure 6. In the smooth curve case, all generator's fuel-cost curves were divided into three main conditions: smooth and non-smooth fuel-cost curve conditions. The last test case employed a valve-point loading function as shown in Figure 6 (Walters and Sheble, 1993; Yang et al., 1996). The last test case was to employ the system voltage profile as the system objective to be minimized. Fuel cost function of each generator connected to the system is generally given in the form of a valve-point loading function with having a quadratic term in it and is expressed by:

\[
f(P_{Gi}) = A_i + B_iP_{Gi} + C_iP_{Gi}^2 + \left| E_i \sin F_i \left( P_{Gi}^{\min} - P_{Gi} \right) \right| \text{ $\$/h} \tag{19}\]

In this paper, 9-bus and 300-bus test systems as shown in Figures 7 and 8 were used to perform the effectiveness of the proposed method.
Figure 8. IEEE 300-bus test power system (Sanchez, 2009).
Table 1. Simulation results of the 9-bus test system with quadratic fuel-cost function.

<table>
<thead>
<tr>
<th>Statistic</th>
<th>Cost function ($)</th>
<th>SSVD</th>
<th>Execution time (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum</td>
<td>4205.9</td>
<td>4205.9</td>
<td>4205.6</td>
</tr>
<tr>
<td>Mean</td>
<td>4205.9</td>
<td>4205.9</td>
<td>4206.0</td>
</tr>
<tr>
<td>Maximum</td>
<td>4205.9</td>
<td>4206.0</td>
<td>4206.1</td>
</tr>
<tr>
<td>SD</td>
<td>0.00</td>
<td>0.01</td>
<td>0.07</td>
</tr>
</tbody>
</table>

SQP: sequential quadratic programming; EP: evolutionary programming; ATS: adaptive tabu search; SSVD: sum of square of system voltage deviation.

Table 2. Simulation results of the 300-bus test system with quadratic fuel-cost function.

<table>
<thead>
<tr>
<th>Statistic</th>
<th>Cost function ($)</th>
<th>SSVD</th>
<th>Execution time (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum</td>
<td>173426.8</td>
<td>173899.2</td>
<td>174296.1</td>
</tr>
<tr>
<td>Mean</td>
<td>177337.5</td>
<td>174396.0</td>
<td>174693.1</td>
</tr>
<tr>
<td>Maximum</td>
<td>182345.0</td>
<td>174689.1</td>
<td>175498.4</td>
</tr>
<tr>
<td>SD</td>
<td>3381.3</td>
<td>168.7</td>
<td>282.7</td>
</tr>
</tbody>
</table>

SQP: sequential quadratic programming; EP: evolutionary programming; ATS: adaptive tabu search; SSVD: sum of square of system voltage deviation.

of the proposed methods. The SQP used in these tests is of MATLAB optimization toolbox. Limits of voltage magnitudes for voltage-controlled buses and limits of tap setting for ULTCs used for all test cases were 0.95 to 1.05 p.u. and 0.90 to 1.10 p.u., respectively.

More careful assessments are needed to confirm the performance of the proposed method. In this paper, the IEEE 9-bus and IEEE 300-bus test systems with 5 and 244 control variables, respectively, were used for the test with two fuel-cost functions and one voltage deviation minimization. For voltage profile calculation, the sum of the square of system voltage deviation (SSVD) was expressed as follows:

\[
SSVD = \sum_{i=1}^{N_{\text{CB}}} (V_{\text{rated}} - V_i)^2
\]  

(20)

where \( V_{\text{rated}} = 1.00 \) p.u. and CB denotes controlled buses

Smooth fuel-cost function (Quadratic case)

In this circumstance, a quadratic fuel-cost function was assigned to all generators. The test was performed on an Intel® 1.7 GHz, 1.0 GB RAM with MATLAB. It was noted that all optimization methods used in this test was performed with 40 computational trials per method. The SQP used in these tests is of MATLAB optimization toolbox. The parameter setting for the SQP was fixed as follows:

1. Tolerance for control variables = \( 1 \times 10^{-4} \)
2. Tolerance for objective function = \( 1 \times 10^{-8} \)
3. Termination criterion for constraint violation = \( 1 \times 10^{-6} \)
4. Maximum number of function evaluation = (100 \times total number of control variables).

Referring to the EP algorithm (Yang et al., 1996; Lai and Ma, 1995; Yuryevich and Wong, 1999), EP parameters used in this paper are given as:

1. Total number of population \( N_P = 30 \)
2. Mutation scaling factor \( \beta = 0.03 \)
3. Maximum number of generation = 1000
4. Termination criterion for the change of the objective function is set to \( 1 \times 10^{-8} \).

For the TS, all parameters that give the best results are given as:

1. Total number of neighbourhood, \( N_{\text{H}} = 10 \)
2. Radius of neighbourhood, \( r = 0.1 \)
3. Maximum number of generation = 1000
4. Termination criterion for the change of the objective function is set to \( 1 \times 10^{-8} \).

As shown in Tables 1 and 2, the SQP can find the lowest
Table 3. Simulation results of the 9-bus test system with non-smooth fuel-cost function.

<table>
<thead>
<tr>
<th>Statistic</th>
<th>Cost function (℅)</th>
<th>SSVD</th>
<th>Execution time (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum</td>
<td>4559.4</td>
<td>4592.8</td>
<td>4589.9</td>
</tr>
<tr>
<td>Mean</td>
<td>4758.6</td>
<td>4662.5</td>
<td>4682.1</td>
</tr>
<tr>
<td>Maximum</td>
<td>5257.7</td>
<td>4799.1</td>
<td>4820.7</td>
</tr>
<tr>
<td>SD</td>
<td>158.5</td>
<td>49.9</td>
<td>61.5</td>
</tr>
</tbody>
</table>

SQP: sequential quadratic programming; EP: evolutionary programming; ATS: adaptive tabu search; SSVD: sum of square of system voltage deviation.

Table 4. Simulation results of the 300-bus test system with non-smooth fuel-cost function.

<table>
<thead>
<tr>
<th>Statistic</th>
<th>Cost function (℅)</th>
<th>SSVD</th>
<th>Execution time (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum</td>
<td>211062.7</td>
<td>233487.2</td>
<td>240813.9</td>
</tr>
<tr>
<td>Mean</td>
<td>288970.8</td>
<td>256222.5</td>
<td>259738.9</td>
</tr>
<tr>
<td>Maximum</td>
<td>310574.6</td>
<td>282472.6</td>
<td>269542.3</td>
</tr>
<tr>
<td>SD</td>
<td>25129.8</td>
<td>14275.3</td>
<td>7287.0</td>
</tr>
</tbody>
</table>

SQP: sequential quadratic programming; EP: evolutionary programming; ATS: adaptive tabu search; SSVD: sum of square of system voltage deviation.

averaged minimum cost function among them, that is 4205.9 ℅ with zero SD to indicate its accuracy. Although, the EP can reach the same amount of averaged minimum cost function, it spent very long computation time (110.1 s for the EP method and 2.0 s for the SQP method). Undoubtedly, the SQP is the best choice of a small 9-bus test system with quadratic fuel-cost function in the execution time and minimum cost considerations. In this case, the voltage profiles of the three methods are not significantly different. Table 2 represents simulation results of the 300-bus system. The solution obtained by EP method is the best among the three methods (177.34 × 10^3 ℅, 174.40 × 10^3 ℅ and 174.69 × 10^3 ℅ for SQP, EP and ATS, respectively), but it spent a long execution time (5035.7, 3787.0 and 754.3 s for SQP, EP and ATS, respectively). So that, the ATS is comparatively better with slightly higher minimum cost function found than those found by the EP but remarkably about 5-time faster calculation time. However, the SSVD of the solution obtained by the ATS method is relatively high.

Non-smooth fuel-cost function (Valve-point loading case)

This test case used non-smooth fuel-cost curves (Figure 6) to produce system complexity. In this circumstance, there exist many local minima that can effectively trap an inefficient search method. All proposed methods still hold their parameter settings with 40 computational trials as previously described. To assess the effectiveness among them, their simulation results are compared in both accuracy and calculation speed as illustrated in Tables 3 and 4, respectively.

The results show that, for the 9-bus system, the EP can again obtain the lowest minimum cost function (4758.6, 4662.5 and 4682.1 ℅ for SQP, EP and ATS, respectively). It also reveals that the solution found by the SQP method is far from a true global minimum. Therefore, it is not appropriate to apply this technique to such a test case. In this test case, the ATS still performed a solution finding with outstanding execution time with satisfactorily accurate results. For the 300-bus system, when comparing the averaged minimum costs obtained among the methods, the EP is the best method (288.97 × 10^3 ℅ for the SQP, 256.22 × 10^3 ℅ for the EP and 259.74 × 10^3 ℅ for the ATS). However, with calculation time comparison, the ATS method can obtain the solution with the fastest calculation time consumed (477.69 s), while the others are very far behind (5085.9 and 2406.6 s for the SQP and EP, respectively).

Sum of square of voltage deviations and power losses

The characterization of system voltage profiles for the test systems was given by the sum of square of voltage
Table 5. Simulation results of the 9-bus test system for SSVD minimization.

<table>
<thead>
<tr>
<th>Statistic</th>
<th>SSVD (p.u.)</th>
<th>Cost function ($)†</th>
<th>Cost function ($)*</th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum</td>
<td>0.00056334</td>
<td>4265.2</td>
<td>4935.7</td>
</tr>
<tr>
<td>Mean</td>
<td>0.00056615</td>
<td>4295.2</td>
<td>5388.6</td>
</tr>
<tr>
<td>Maximum</td>
<td>0.00057324</td>
<td>4325.9</td>
<td>5947.0</td>
</tr>
<tr>
<td>SD</td>
<td>0.00000252</td>
<td>15.3</td>
<td>271.3</td>
</tr>
</tbody>
</table>

†Valve-point loading fuel-cost function; *Quadratic fuel-cost function. SSVD: sum of square of system voltage deviation.

Table 6. Simulation results of the 300-bus test system for SSVD minimization.

<table>
<thead>
<tr>
<th>Statistic</th>
<th>SSVD (p.u.)</th>
<th>Cost function ($)†</th>
<th>Cost function ($)*</th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum</td>
<td>0.0075</td>
<td>193205.2</td>
<td>292145.5</td>
</tr>
<tr>
<td>Mean</td>
<td>0.0119</td>
<td>203574.9</td>
<td>318387.5</td>
</tr>
<tr>
<td>Maximum</td>
<td>0.0182</td>
<td>218945.4</td>
<td>348515.6</td>
</tr>
<tr>
<td>SD</td>
<td>0.0026</td>
<td>5845.0</td>
<td>14333.3</td>
</tr>
</tbody>
</table>

†Quadratic fuel-cost function; *Valve-point loading fuel-cost function. SSVD: Sum of square of system voltage deviation.

Table 7. Comparison of power losses, fuel cost and SSVD minimization for the 9-bus test system with quadratic fuel-cost function.

<table>
<thead>
<tr>
<th>System profile</th>
<th>Objective function</th>
<th>Power loss</th>
<th>Fuel-cost</th>
<th>SSVD</th>
</tr>
</thead>
<tbody>
<tr>
<td>Power losses (MW)</td>
<td>2.32</td>
<td>2.73</td>
<td>3.12</td>
<td></td>
</tr>
<tr>
<td>Cost function ($)</td>
<td>4232.4</td>
<td>4206.0</td>
<td>4297.5</td>
<td></td>
</tr>
<tr>
<td>SSVD (p.u.)</td>
<td>0.0496</td>
<td>0.0491</td>
<td>0.0006</td>
<td></td>
</tr>
</tbody>
</table>

SSVD: Sum of square of system voltage deviation.

deviations as previously described in Equation 20. Here, all control variables were adjusted to gain a minimum voltage deviation for the whole system as good as possible. The aim of this test is to verify that the solutions obtained according to the given objectives in the first two test cases can give a satisfactory system voltage profiles or not. To precede the test, the fuel-cost function was replaced by the SSVD as the new objective function. It notes that this test case was carried out to collect the test results when compare with the solutions obtained by minimizing cost functions. So, only the ATS method was selected to precede the test due to the shortest execution time with the satisfactorily accurate solution. All simulation results of this section are shown on Tables 5 and 6 for the two respective test systems.

As can be seen, it is clear that the minimum cost function and the minimum voltage deviation are mutually exclusive. While minimizing the system voltage deviation, the cost function was significantly raised (4206.0 and 4295.2 \$ for fuel-cost and SSVD minimization, respectively, in the case of the 9-bus system with quadratic fuel-cost function). The same trends can be found for the 300-bus test case and the case of valve-point loading fuel-cost function.

In addition, the comparison among power loss, fuel-cost and SSVD minimization of the 9-bus test system was investigated and put on Table 7 for more explanations. Table 7 illustrates system performances when minimizing some particular objective. It is obvious that the minimum of the three functions is mutually exclusive. It critically depends on the true main objective of a problem itself. For example, in electrical power generation and transmission viewpoint, the fuel-cost function in general acts as the main criterion to operate the system with system voltage profiles being inequality constraints.
In some particular power feeding systems like alternate current (AC) railway power distribution systems (Hill, 1994; Goodman et al., 1998), where electric power is fed at the substation point, there was no generation cost, therefore system voltage deviation becomes obviously critical. Although, the AC railway feeding systems can operate with about ±30% voltage deviations (White, 1997), it also affects traction drive performances (Hill, 1994b, 1994c), voltage stability and limitation of feeding capacity to railway power systems. Thus, the SSVD minimization is more attractive for this case.

To picture system voltage profiles of the fuel-cost minimization, some test results were selected and presented in Figures 9 and 10, comparatively with the system voltage profile obtained by minimizing SSVD.

DISCUSSION

For decades, there have been many publications related to solution methods for searching OPF solutions. Many methods either classical or evolutionary optimizations have been continually developed and widely published. This research proposes comparative studies to lead some key conclusions for selecting an appropriate optimization method applied to the OPF problem.

As can be seen, when many local minima exist, typically a non-convex problem, the SQP does not fit to such a circumstance according to their trapped local minimum found. Among the three methods, EP is suitable for a problem that needs very accurate results but does not attend calculation speed. Nonetheless, for a small-scale, convex OPF problem like a small 9-bus power system, the SQP can guarantee that the solution obtained is the global minimum and also provides satisfactory calculation speed, but does not for a large-scale system.

In literature (Lai and Ma, 1995; Wong, 1997; Yuryevich and Wong, 1999; Tangpatiphan and Yokoyama, 2008, 2009), the execution time consumed by the SQP is...
Figure 10. System voltage profile of each test case for the 9-bus test system.

roughly 1/6 of that of the EP. However, this estimated CPU time is evaluated on the IEEE 30-bus test system. For a smaller-sized test system, e.g. 6-bus, 14-bus, etc., the execution time of the SQP can be as fast as 1/10 of that of the EP while a larger-sized test system gives a contrary results. In this work, results from the small 9-bus test system show that the execution times taken by the SQP are 1/55 and 1/12 of those required by the EP for smooth quadratic and non-smooth fuel-cost cases, respectively. In the IEEE 300-bus test system, the SQP consumes longer execution time than that required by the ATS, 20/3 and 10 of the execution time consumed by the SQP for smooth quadratic and non-smooth fuel-cost cases, respectively. This confirms the effectiveness of the ATS for solving non-smooth fuel-cost cases of optimal power flow in the large 300-bus test system.

Conclusion

The ATS is of course like the EP in which to obtain a near global minimum is dependent on their parameter settings and termination criteria. But its calculation time is remarkably less than that spent by the EP or even the SQP for the 300-bus system. In a very complicated OPF
problem like the second test system with 244 control variables (68 for generation output, 69 for voltage magnitudes and 107 for ULTCs), the ATS can completely escape a deadlock from local minima to reach a near global minimum that other search methods cannot or spend too much calculation time to do so. For applications that need highly accurate solutions, the ATS’ parameters can be easily tuned to achieve the requirement at the expense of long calculation time.

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REFERENCES
